# B.Sc. (Mathematics) (Part I) (Level 4.5)(Semester – I) (NEP-2020)

#### Syllabus to be implemented from Academic Year 2024-25

Course type

DSC - II

Title of course

: Calculus

Credit

: 02

Course Learning Outcomes: Upon successful completion of the course students will able to:

- CO 1. find higher derivatives of product two differentiable functions using Leibnitz theorem.
  - CO 2. learn conceptual variations while advancing from one variable to several variables in calculus.
  - CO 3. understand the consequences of mean value theorems for differentiable functions.
  - CO 4. apply L' Hôpital's rule to various indeterminate forms.

### Unit - 1: Differentiation

(15 hrs.)

- 1.1. Successive Differentiation
  - 1.1.1. Higher order derivatives: notations.
  - 1.1.2. Calculation of nth derivative: Standard results
  - 1.1.3. Determination of n<sup>th</sup> derivative of rational functions: Examples.
  - 1.1.4. The n<sup>th</sup> derivative of product of the powers of sine and cosines: Examples.
  - 1.1.5. Leibnitz's Theorem. The n<sup>th</sup> derivative of product of two functions.
  - 1.1.6. Examples on Leibnitz's Theorem.
- 1.2. Partial differentiation
  - 1.2.1. Introduction to functions of two and more variables
  - 1.2.2. Partial derivative: first order and higher order examples.
  - 1.2.3. Geometrical interpretation of partial derivatives of first order.

## Unit - 2: Mean Value Theorems and Indeterminate forms

(15 hrs.)

- 2.1. Mean Value Theorems
  - 2.1.1. Rolle's Mean Value Theorem, Geometrical interpretation.
  - 2.1.2. Lagrange's Mean Value Theorem, Geometrical interpretation.
  - 2.1.3. Meaning of sign of derivative
  - 2.1.4. Cauchy's Mean Value Theorem.
  - 2.1.5. Examples on 2.1.1, 2.1.2, 2.1.3 and 2.1.4
- 2.2. Indeterminate forms
  - 2.2.1. Indeterminate forms: L' Hôpital's rule for  $\frac{0}{0}$  and  $\frac{\infty}{\infty}$  form (Statement only).
  - 2.2.2. The indeterminate forms  $0 \times \infty$ ,  $\infty \infty$ ,  $0^0$ ,  $1^\infty$ ,  $\infty^0$
- 2.3. Expansion of functions
  - 2.3.1. Maclaurin's theorem (statement only): Examples.
  - 2.3.2. Taylor's theorem (statement only): Examples.

## Recommended Books:

 Differential Calculus, Shanti Narayan and P.K. Mittal, S. Chand publishing, 15th edition (2016).

Scope:

Unit 1 - 1.1: Chapter 5: 5.1 to 5.5

1.2: Chapter 11: 11.6, 11.6.1, 11.7.1

Unit 2 - 2.1: Chapter 8: 8.1, 8.2, 8.3, 8.5

2.2: Chapter 10: 10.1 to 10.6

2.3: Chapter 6: 6.1, 6.2

#### Reference Books:

- 1. Differential Calculus, Gorakh Prasad, Pothishala Pvt. Ltd., 19th edition (2016).
- 2. Aspects of Calculus, Gabriel Klambauer, Springer-Verlag (1986).
- 3. Differential Calculus, Hari Kishan, Atlantic Publishers & Dist. (2007).
- 4. Calculus, George B. Thomas Jr., Joel Hass, Christopher Heil & Maurice D. Weir, Pearson Education, 14<sup>th</sup> edition (2018).